**­­**

**PiXL Independence:**

**Mathematics** –Answer Booklet

KS4 HIGHER

**Topic 2 – Powers and Roots, HCF/LCM. Ratio and Proportion.**

1. **Basic Skills Check**

*Answer the following questions. In order to improve your basic arithmetic you should attempt these without a calculator where possible.*

**Skills Check 1**

1. A phone is reduced by 15% to a price of £140.25. Calculate the original cost of the system.

£165

1. What is $\frac{2 }{3}$ of £540? 360
2. Write 26 as a product of its prime factors. 2 x 13
3. Factorise x² -2x -24. (x-6) (x+4)
4. Write 620,000,000 in standard form. 6.2 x 108
5. Solve: $2x+7\leq -11. x\leq -9$
6. Use prime factors to find the lowest common multiple of 170 and 80.

LCM = 1360

HCF = 10

1. List the first 5 terms of the sequence 4n- 2.

2, 6, 10, 14, 18

1. Find the total perimeter of the sector shown, correct to one decimal place.

Sector length = 9.076

130˚

Total length = 17.1 cm (1dp)

4cm

1. Calculate , giving your answer in standard form correct to **two** significant figures.

2.4 x 106

**Skills Check 2**

1. A year ago Peter was 152 cm. He is now 4% taller. How tall is Peter now? 158.08cm

2. Calculate , giving your answer in standard form correct to two significant figures.

 1.1 x1016

3. Write 48 as a product of prime factors. What is the LCM of 48 and 54?

 HC F= 6, LCM = 432

4. Factorise x² -20x + 96.

 (x-8) (x-12)

5. Write 0.000000754 in standard form.

7.54 x 10-7

6. Solve: $-19\leq 6-5x$

 $5\geq x$

1. Calculate the total surface area of a cylinder with radius 4cm and length 12cm. Give your **final** answer to one decimal place.

12cm

4cm

Circles = 16$π$ x 2

Curved surface area = 96π

Total SA = 128π

= 402.1cm2

1. Find the nth term of the sequence: 4, 7, 12, 19,….

 $n^{2}+3$

1. Find the reciprocal of the number 2.8, giving your answer as a fraction.

 $\frac{5}{14}$

1. A class of 14 boys and 18 girls take a test. The mean mark for the boys is 65%., and the mean mark for the girls is 80%. Calculate the mean mark for the whole class.

73.4% (1dp)

**Skills Check 3**

1. A shopkeeper buys small scooters at £45. She sells the bikes making 15% profit. Calculate the selling price of the scooters.

£51.75

1. George uses ¾ of a tin of dog food each day. How many tins does he use in 7 days?

 5 $\frac{1}{4}$ so opens 6 tins

1. Find the HCF of 48 and 16.

16

1. Factorise x² + x -30.

(x+6) (x-5)

5. Write 0.0000000758 in standard form.

* 1. X 108

6. Solve: $5x+7\geq 3x-2$

$$x\geq 4.5$$

7. Find the total perimeter of the sector shown, correct to one decimal place.

125˚

7cm

 $\frac{125}{360}×14π +14 =29.3cm$

8. Find the nth term of the sequence: -1, 2, 7, 14

 $n^{2}-2$

9. Use prime factors to find the highest common factor of 250 and 904.

2

10. A class of 12 boys and 18 girls take a test. The mean mark for the class is 75%. If the mean mark for the boys is 64%, find the mean mark for the girls.

 82.3%

1. **Short Exam Questions**

**Section 1**

1. Simplify each of these expressions, giving each answer in the form yn:
	1.  $y^{8}$
	2.  $y^{1/3}$
	3.  $y^{-2}$
	4.  $y^{-12}$
	5.  $y^{9}$
	6.  $y^{2}$
2. Evaluate each of the following:
	1.  $3$
	2.  $1/144$
	3.  $1$
	4.  $81$
	5.  $1/7$
3. Write each of the following as powers of 8:
	1.  $8^{-1}$
	2. 2 $8^{1/3}$
	3. 1 $8^{0}$
	4.  $8^{-2}$

Solve these exponential equations.

* 1.  $x=1$
	2.  $x=1$/2
	3.  $x=-2$
1. Expand the brackets and simplify the following expressions as far as possible:
	1.  $8+6\sqrt{3}$
	2.  $8-2\sqrt{7}$
	3.  9
2. Simplify these expressions as far as possible by first ‘rationalising the denominator’ in each case:
	1.  $\frac{12\sqrt{3}}{3}=4\sqrt{3}$
	2.  $\frac{30\sqrt{6}}{6}=5\sqrt{6}$
	3.  $\frac{12\sqrt{3}}{3}=4\sqrt{3}$

**Section 2 - HCF/LCM**

1. Drummers hit their drums on certain beats. Drummer A hits his drum every 6 seconds. Drummer B hits his drum every 7 seconds. In the first 60 seconds, will they ever play at the same time?

Yes at 42 seconds

1. Are these correct? If not correct them.
a) HCF of 21 and 28 is 7 b) HCF of 27 and 45 is 5 c) HCF of 28 and 16 is 8.

	1. correct b) 9 c) 4
2. a) Write 48 and 120 in prime factor form.

$$2^{4}×3=48$$

 $2^{4}×3=120$

 b) Use your answers to find their highest common factor.

HCF = 24

1. As a product of prime factors 60 = 22 x 3 x 5.
a) What number is represented by 2 x 32 x 5?

 90
b) Find the lowest common multiple of 60 and 48.

 LCM=240

1. Tom, Sam and Matt are counting drum beats.
Tom hits a snare drum every 2 beats.
Sam hits a kettle drum every 5 beats.
Matt hits a bass drum every 8 beats.

Will they ever play at the same time during 60 beats?

Yes, at the 40th beat, because the LCM of all three numbers is 40

1. “I am thinking of two numbers, the HCF of the two numbers is 2. The LCM is 210” what could my numbers be? Possible answers 10,42 or 30,1 or 70,6
2. Using prime decomposition find the LCM and HCF for 240 and 36.

LCM = 720 HCF = 12

1. Hotdogs come in jars of 8 and cost £1.20 per jar. Bread rolls are in packs of 12 and cost 99p. How many do I need to buy so I have exactly the same number of hotdogs and bread buns and how much will that cost?

LCM of 8 and 12 = 48

So I need 6 packs of hotdogs and 4 packs of rolls.

Total cost: (6 x 1.20) + (4 x 0.99) = £11.16

**Section3 - Ratio and Proportion**

1. V is inversely proportional to h. It is known that V = 18 when h = 24.
	1. Find the equation that connects V and h.
	2. Find V when h = 15.
	3. Work out h when V = 30.

a.$ V=\frac{k}{h} so 18=\frac{k}{24} so k=18×24=432 so $ $V=\frac{432}{h}$

b. $V=\frac{432}{15}=28.8$

c. $30=\frac{432}{h} so h=\frac{432}{30}=14.4 $

1. T is directly proportional to r3. It is known that T = 36 when r = 2.
	1. Find the equation that connects T and r.
	2. Find T when r = 6.
	3. Work out r when T = 7776.

a.$ T=kr^{3} so 36=k×2^{3} so k=4.5 so $ $T=4.5r^{3}$

b. $T=4.5×6^{3}=972$

c. $7776=4.5×r^{3} so r^{3}=\frac{7776}{4.5}=1728 so r=\sqrt[3]{1728}=12 $

1. On a map, the distance between two cities is 15cm. In real-life the distance is known to be 75km.

Find the scale of the map, giving your answer in the form 1 : n.

15cm : 75km = 1cm : 5km = 1cm : 5000m = 1cm : 500,000cm = **1 : 500,000**

1. In a school, the ratio of boys to girls is 4 : 5. If there are 424 boys in the school, how many girls are there? 424 = 4 parts

106 = 1 part

530 girls

1. Graham and Harry agree to share their weekly earnings of £748 in the ratio 3 : 5. How much will each of them receive?

Graham = £280.50

Harry = £467.50

1. Simplify each of these ratios as far as possible.
	1. 2kg : 800g 5:2
	2. 45 minutes : 2 hours 3:8
	3. 800mm : 40cm : 2metres. 2:1:5
2. Write the ratio 50 : 120 in the form 1 : n.

1:2.4

1. Write 240 : 600 in the form n : 1.

0.4:1

1. On a map, the distance between two towns is 12cm. In real-life the distance is known to be 18km. Find the scale of the map, giving your answer in the form 1 : n.

1:150000

1. The cost of a certain type of carpet roll is directly proportional to the length bought. Sheila pays £17.55 for 3 metres of this carpet.
	1. Write a formula to give the **cost** in terms of the **length** of carpet.

 C=5.85L

* 1. If Wayne buys 8 metres of the same carpet, how much will it cost?

 £46.80

1. P is directly proportional to t2. It is known that P = 20.8 when t = 4.
	1. Find the proportionality equation that connects P and t. p = kt2

20.8 = k x 16

K = 1.3

P = 1.3t2

* 1. Use your equation to find P when t = 9. P = 1.3 x 81

P = 105.3

* 1. Find the value of t when P = 520. 520 = 1.3 x t2

T = 20

1. R is inversely proportional to d. When d = 36, R = 4.
	1. Find the proportionality equation connecting R and d. $ R=\frac{k}{d}$

$$4=\frac{k}{36}$$

 $k=144$

* 1. Use this equation to find R when d = 10. $R=\frac{144}{10}$

R = 14.4

* 1. Calculate d when R = 1.5. $1.5=\frac{144}{d}$

$$d=96$$

**Section4 - Mixed Questions**

1. Three litres of diesel costs £2.82. What is the cost of 40 litres? £37.60
2. 300 grams of sweets cost £1.65. Find the cost of

a) 100 grams of sweets 55p
b) 500 grams of sweets £2.75

c) 5 kg of sweets. £27.50
Why might your answer to (c) be unrealistic? 5KG of sweets is a lot

1. a) Elana is paid £12.50 per hour. She is given a pay rise of 20%. What is her new pay rate? £15 ph
b) Six months later, due to adverse economic conditions Elana is asked to take a 20% pay *cut*.
 What will be her hourly rate now?

 £12 ph (NOT £12.50….. why??)

1. Explain why 0.28 must be a rational number.

. Can be written as a fraction so must be rational.

1. Without a calculator evaluate each of these
2. $64^{\frac{2}{3}}$ b. $5^{-2}$ c. $18^{0}$

 a.  b.  c. 1

1. Simplify as far as possible;
2. $\sqrt{18}+ \sqrt{50}$ b. $(3+\sqrt{7})(4-\sqrt{7})$

 $8\sqrt{2}$ $5+\sqrt{7}$

1. Simplify these by first rationalising the denominator.
2. $\frac{12}{\sqrt{6}}$ b. 

$2\sqrt{6}$ $4(3+\sqrt{3})$

1. A rectangle has an area of 8cm2. If its width is cm, calculate its perimeter, giving your answer in the form cm where *A* and *B* are integers.

Rectangle length = cm

Perimeter = cm

1. On Saturday the ratio of adults to children in a swimming pool is 2:3. The swimmers are either in the main pool or on the slides. $\frac{1}{3}$ of the children are on the slides. 68 children are in the main pool.

How many people went swimming in total?

2/3 = 68

1/3 = 34 children

Total children = 102

102 = 3 ‘parts’ from the ratio so 1 part = 32.

Total adults = 68

Total people =170

****

**Commissioned by The PiXL Club Ltd.**

This resource is strictly for the use of member schools for as long as they remain members of The PiXL Club. It may not be copied, sold, or transferred to a third party or used by the school after membership ceases. Until such time it may be freely used within the member school.

All opinions and contributions are those of the authors. The contents of this resource are not connected with, or endorsed by, any other company, organisation or institution.

PiXL Club Ltd endeavour to trace and contact copyright owners. If there are any inadvertent omissions or errors in the acknowledgements or usage, this is unintended and PiXL will remedy these on written notification.