

November 2017 paper 3

① $150 < h \leq 160$ $160 - 170 \quad \frac{80}{2} = 40$

B1

which interval contains
 40^{th} value

b) plot mid-point against frequency
join with straight lines

C2

② London 1 L = 108.9 p or £1.089

US 1 gallon = \$ 2.83

£ $\xrightarrow{\times 1.46}$ \$
 $\xleftarrow{\div 1.46}$

gallons $\xrightarrow{\times 3.785}$ Litres
 $\xleftarrow{\div 3.785}$

• We must compare Like with Like

• I am choosing L in pence and so will change the US into L and pence.

US

1 gallon : \$ 2.83

\nearrow
3.785 L

\nwarrow
 $\$ 2.83 \div 1.46$
 $= \pounds 1.93835 \dots$

P1

3.785 L : £1.93835

$\swarrow \div 3.785$

1 L : £0.512115.....

$\searrow \div 3.785$

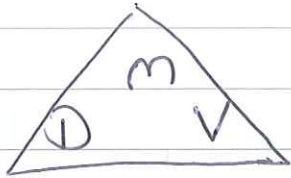
P1

London 1 L = 108.9 p

US 1 L = 51.2 p

The petrol is better value for money in the US
as it is 57.7 p cheaper per Litre C1

Question 3



$$D = 19.3 \text{ g/cm}^3$$
$$M = 12500 \text{ g}$$
$$V =$$

$$(12.5 \text{ kg} \times 1000) \text{ MI}^*$$

* notice density given in g/cm^3 but volume in kg
change volume into grams

$$V = \frac{M}{D} = \frac{12500}{19.3} = 647.668 \dots$$

MI

$$= \underline{648 \text{ cm}^3} \text{ (3sf) AI}$$

Question 4

Blue : Green

Green : Red

2 : 5

4 : 1

x4

x4

x5

x5

make Green
same number

8 : 20

20 : 5

PI

so now we have

Blue : Green : Red

8 : 20 : 5

x3

x3

x3

PI

33 pens

x3

24 : 60 : 15

99 pens

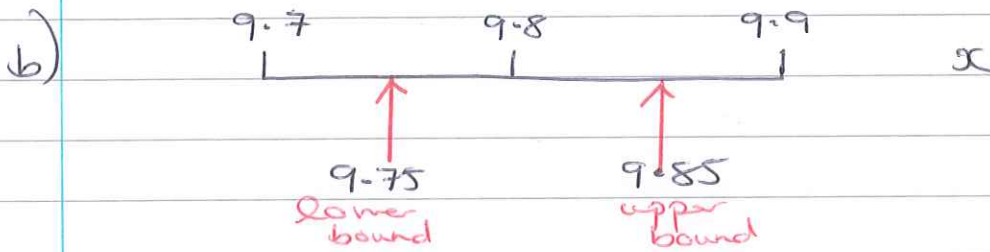
this is less than
100

greatest possible number of Red pens is 15

AI

Question 5

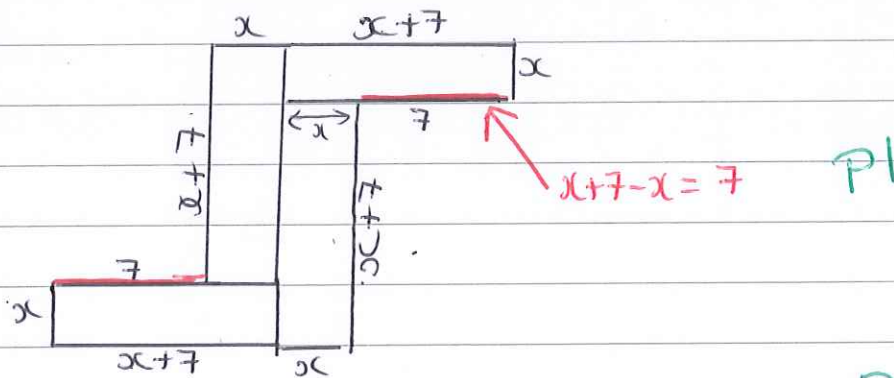
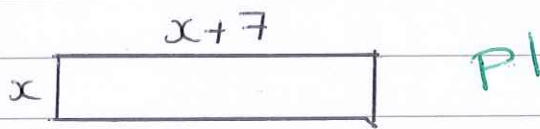
a) $\frac{1}{1.6} = 0.625$ BI (or $\frac{5}{8}$) "...answer as a decimal"



error interval

$$\underline{9.75 \leq x < 9.85} \quad \text{BI}$$

Question 6

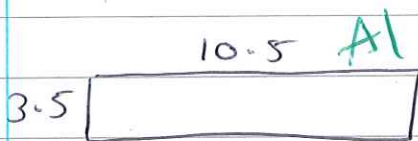


Perimeter $x + x+7 + x + x+7 + x + x+7 + x + x+7 + 7 + 7 = 70$

$$8x + 42 = 70$$

$$8x = 28$$

$$\underline{x = 3.5}$$



Area one rectangle = 3.5×10.5
 $= 36.75 \text{ cm}^2$

Area 8-sided shape = $4 \times 36.75 \text{ cm}^2$
 $= \underline{147 \text{ cm}^2}$

BI

Question 7

$$(13.8 \times 10^7) \times (5.4 \times 10^{-12})$$

$$= 7.452 \times 10^{-4} \quad M1$$

$$= 0.0007452$$

$$\underline{0.0007452} \quad A1$$

Question 8

a) Mel's because she has carried out the most number of trials B1

b) Total number of trials = 150
Total number of point DOWN = 100
Total number of point UP = 50

	Lucy	Mel	Tom	Total
point DOWN	31	53	16	100
point UP	14	27	9	50
Total	45	80	25	150

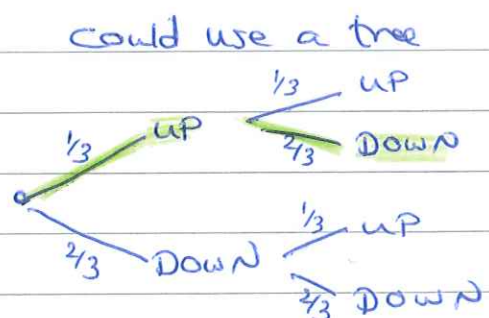
$$P(\text{point DOWN}) = \frac{100}{150} = \frac{2}{3}$$

$$P(\text{point UP}) = \frac{50}{150} = \frac{1}{3}$$

$P(\text{point UP } 1^{\text{st}} \text{ AND point DOWN } 2^{\text{nd}})$

$$= \frac{2}{3} \times \frac{1}{3} \quad M1$$

$$= \underline{\underline{\frac{2}{9}}} \quad A1$$



Question 9

a) new boat £12 500

$$n=0, V=12500$$

$$V = 12500 \times (0.85)^n$$

$$n = ?, V < \frac{12500}{2}$$

After how many years is Jack's boat worth less than £6250

Use trial and improvement

try 5 years, $n=5$, $V = 12500 \times 0.85^5$
 $= £5546.32 < £6250$
ml

try 4 years, $n=4$, $V = 12500 \times 0.85^4$
 $= £6525.08 > £6250$

5 years A!

Could try a more systematic approach

$$n=1, V = 12500 \times 0.85^1 = £10625$$

$$n=2, V = 12500 \times 0.85^2 = £9031.25$$

$$n=3, V = 12500 \times 0.85^3 = £7676.56$$

$$n=4, V = 12500 \times 0.85^4 = £6525.08$$

$$n=5, V = 12500 \times 0.85^5 = £5546.32$$

5 years

$$\begin{aligned}
 \text{Interest} &= R\% \text{ of } \pounds 5500 \\
 &= \frac{R}{100} \times 5500 \\
 &= \frac{5500R}{100} \\
 &= \underline{55R \text{ Interest}}
 \end{aligned}$$

$$\begin{aligned}
 \text{Tax} &= 40\% \text{ of } 55R \\
 &= 0.4 \times 55R \\
 &= \underline{22R \text{ Tax}}
 \end{aligned}$$

$$\begin{aligned}
 \text{Interest} - \text{Tax} &= \pounds 79.20 \\
 55R - 22R &= 79.20 \\
 33R &= 79.20 \\
 R &= \underline{2.4}
 \end{aligned}$$

$$R = 2.4\%$$

PI PI AI

I seem to have missed Q10 ??!!

Question 11

$$n = 60$$

a) Median ≈ 57 g BI

b) He may not be correct as if the data was grouped we cannot be certain that the smallest was 40kg and the biggest was 80kg

c) UQ ≈ 63 kg cl. \therefore 25% of potatoes weigh more than 63kg

d) 11 potatoes weigh more than 65kg which is $\frac{11}{60} \times 100 = 18.33\%$ \therefore less than 25% weigh more than 65kg

Question 12

$$P(\text{Red Red}) = 0.25 \times 0.6 = 0.15$$

Let n represent the number of the times the spinner B spun

$$0.15 \times n = 24$$

$$0.15n = 24$$

$$n = 160 \quad \text{M1}$$

The spinner has been spun 160 times

$$P(\text{White White}) = 0.75 \times 0.4 = 0.3 \quad \text{M1}$$

Number of times both land on white

$$\approx 0.3 \times 160$$

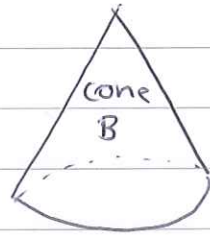
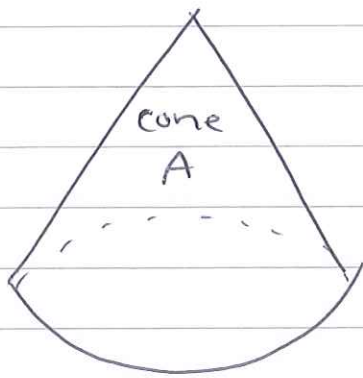
$$= \underline{48 \text{ times}} \quad \text{A1}$$

Question 13

$$x^2 + 6x - 7 \equiv (x+3)^2 - 9 - 7 \quad \text{M1}$$

$$= \underline{(x+3)^2 - 16} \quad \text{A1}$$

Question 14



Volume 27 : 8

$\times \frac{8}{27}$

Scale Factor of Volume $k^3 = \frac{8}{27}$

Scale Factor of Length $k = \sqrt[3]{\frac{8}{27}} = \frac{2}{3}$ M1

Scale Factor of Area $k^2 = \left(\frac{2}{3}\right)^2 = \frac{4}{9}$ M1

Surface Area of Cone A = 297 cm^2

Surface Area of Cone B = $297 \times \frac{4}{9}$ A1
 $= 132 \text{ cm}^2$

Question 15

a) $x^3 + 7x - 5 = 0$

$$x=0, \quad (0)^3 + 7(0) - 5 = -5$$

$$x=1, \quad (1)^3 + 7(1) - 5 = 3 \quad \text{M1}$$

change of sign therefore solution (or root) lies between $x=0$ and $x=1$ C1

b) $x^3 + 7x - 5 = 0$

$$x^3 + 7x = 5 \quad \text{C1}$$

$$x(x^2 + 7) = 5$$

$$x = \frac{5}{x^2 + 7} \quad \text{C1}$$

c) $x_{n+1} = \frac{5}{x_n^2 + 7}$

on calc

$$1 =$$

$$x_0 = 1$$

$$x_1 = 0.625 \quad \text{M1}$$

$$x_2 = 0.67653 \quad \text{M1}$$

$$x_3 = 0.67045 \quad \text{A1}$$

$$\frac{5}{\text{ANS}^2 + 7}$$

$$=$$

$$=$$

$$=$$

d) Subs $x = 0.67045$ into $x^3 + 7x - 5$

to give -0.0054806 (5sf) M1

this is close to zero and therefore is a good answer. C1

Question 16

148 km

147.5 \rightarrow 148.5

11.8 litres

11.75 \rightarrow 11.85

B1

$$\text{Petrol consumption} = \frac{100 \times \text{Litres petrol}}{\text{km travelled}}$$

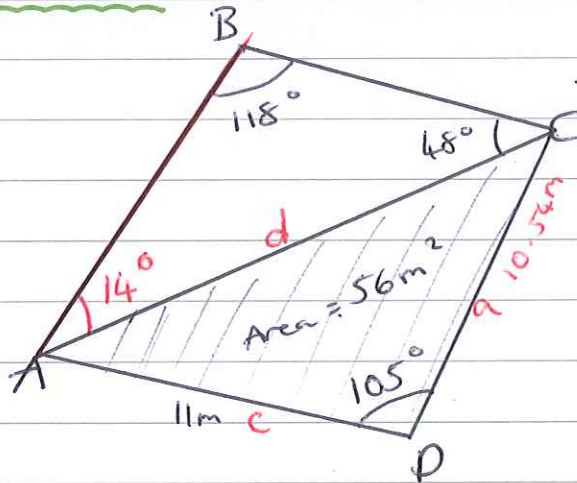
lower bound $\frac{100 \times 11.75^{\text{small}}}{148.5^{\text{big}}} = 7.912 \text{ L/km}$

P1

upper bound $\frac{100 \times 11.85^{\text{big}}}{147.5^{\text{small}}} = 8.034 \text{ L/km}$

A Yes, Nathan could be wrong. It is possible that his car used more than 8 L/km as the upper bound for petrol consumption is 8.034 L/km

Question 17



Area ADC

$$\frac{1}{2} ac \sin D = 56$$

$$\frac{1}{2} (10.54) \times 11 \times \sin 105 = 56 \quad \text{P1}$$

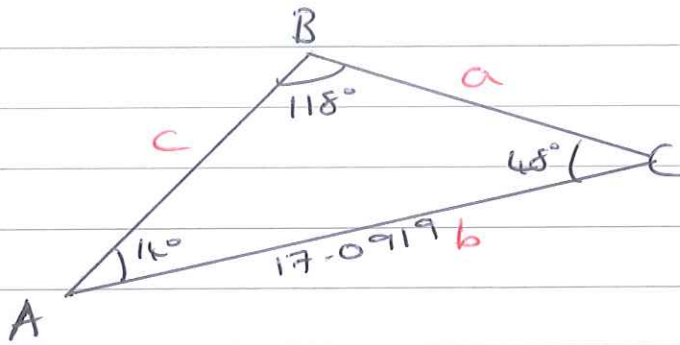
$$5.3126 CD = 56$$

$$\underline{CD = 10.54099} \quad \text{P1}$$

cosine rule to find AC

$$\begin{aligned} d^2 &= a^2 + c^2 - 2ac \cos D \\ &= 10.54^2 + 11^2 - 2(10.54) \times 11 \times \cos 105^\circ \\ &= 292.133 \quad \text{P1} \end{aligned}$$

$$\underline{AC = 17.0919}$$



$$\frac{b}{\sin B} = \frac{c}{\sin C}$$

$$\frac{17.0919}{\sin 118^\circ} = \frac{AB}{\sin 48^\circ}$$

$$\frac{17.0919}{\sin 118} \times \sin 48 = AB \quad \neq 1$$

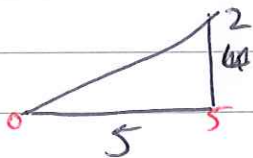
$$14.38563... = AB$$

$$\underline{AB = 14.4 \text{ m (1dp)}} \quad \neq 1$$

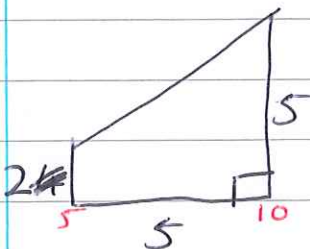
Question 18

Distance travelled = Area under graph

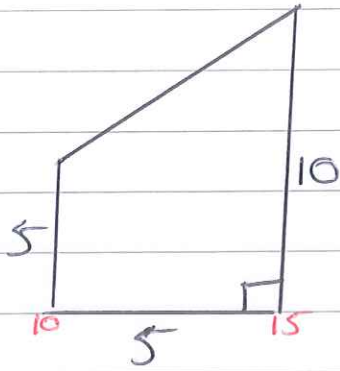
Each strip will be a trapezium (except 1st triangle)



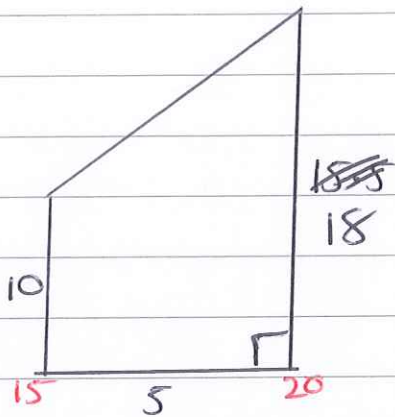
$$\text{Area} = \frac{1}{2} \times 5 \times 2 = 5 \text{ m} \quad \text{m}$$



$$\text{Area} = \frac{1}{2} (2+5) \times 5 = 17.5 \text{ m} \quad \checkmark$$



$$\text{Area} = \frac{1}{2} (5+10) \times 5 = 37.5 \text{ m}$$

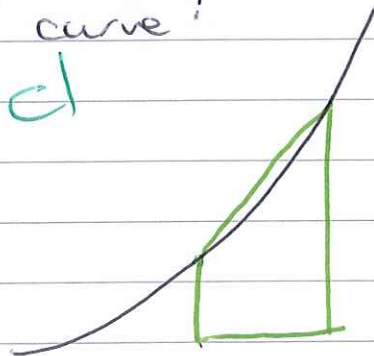


$$\text{Area} = \frac{1}{2} (10+18) \times 5 = 70 \text{ m}$$

① Distance travelled in first 20 seconds,
 $= (5 + 17.5 + 37.5 + 70) \text{ m}$ m
 $= \underline{130 \text{ m}}$ A1

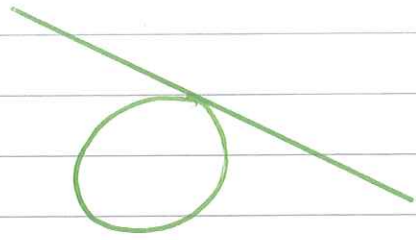
b) Overestimate

The trapezium strips are larger than the space under the curve.



Question 19

line $x - 2y = 10$
circle $x^2 + y^2 = 20$



if the line is a tangent to the circle then
when solving simultaneously $b^2 - 4ac = 0$
OR, there will only be one solution.

$$x = 10 + 2y$$

$$(10 + 2y)^2 + y^2 = 20$$

MI

$$(10 + 2y)(10 + 2y) + y^2 = 20$$

$$MI \quad 100 + 20y + 20y + 4y^2 + y^2 = 20$$

$$MI \quad 100 + 40y + 5y^2 = 20 \quad \begin{matrix} \div 5 \\ \hline \end{matrix}$$

$$20 + 8y + y^2 = 4 \quad \begin{matrix} \div 4 \\ \hline \end{matrix}$$

$$16 + 8y + y^2 = 0$$

$$y^2 + 8y + 16 = 0$$

$$(y + 4)(y + 4) = 0$$

perfect square

$$MI \quad (y + 4)^2 = 0$$

$$y + 4 = 0$$

$$y = -4$$

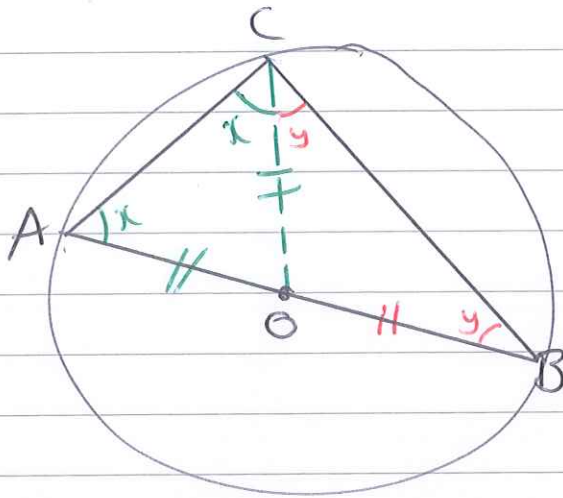
$$x = 10 + 2(-4)$$

$$= 10 - 8$$

$$= 2$$

c/ There is only one solution, therefore $x - 2y = 10$ is
a tangent to the circle $x^2 + y^2 = 20$ touching once
at the point $(2, -4)$

Question 20



$AO = OC$ since radii of circle

\therefore $\triangle AOC$ is an isosceles triangle with equal base angles x

$OB = OC$ since radii of circle

\therefore $\triangle OCB$ is an isosceles triangle with equal base angles y

Angles in triangle ACB add up to 180°

$$\therefore x + (x+y) + y = 180^\circ$$

$$2x + 2y = 180$$

$$2(x+y) = 180$$

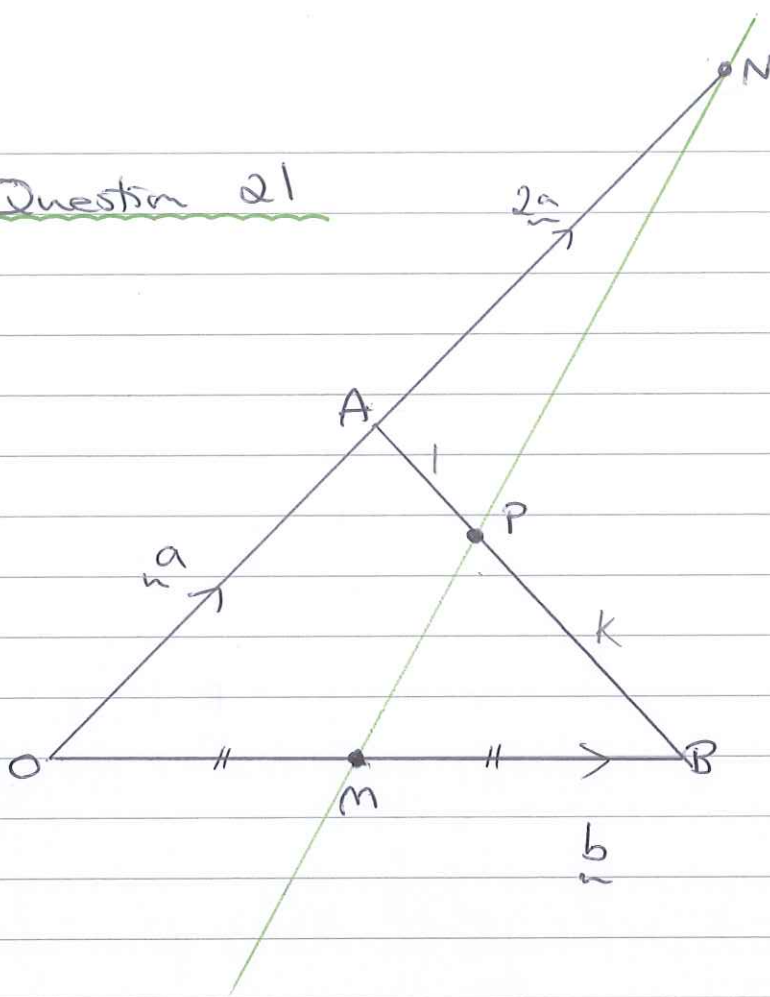
$$x+y = 90^\circ$$

$$\text{Angle } C = x+y = 90^\circ$$

\therefore $\text{Angle } ACB = 90^\circ$

CI reasons

Question 21



$$\vec{AP} = k\vec{AB}$$